

Graphs of the Other Trigonometric Functions

Recall the definitions of the “other trig functions”:

DEFINITIONS: The **tangent function** is defined by $\tan(t) = \frac{\sin(t)}{\cos(t)}$.

The **cotangent function** is defined by $\cot(t) = \frac{1}{\tan(t)}$.

Consequently: $\cot(t) = \frac{\cos(t)}{\sin(t)}$

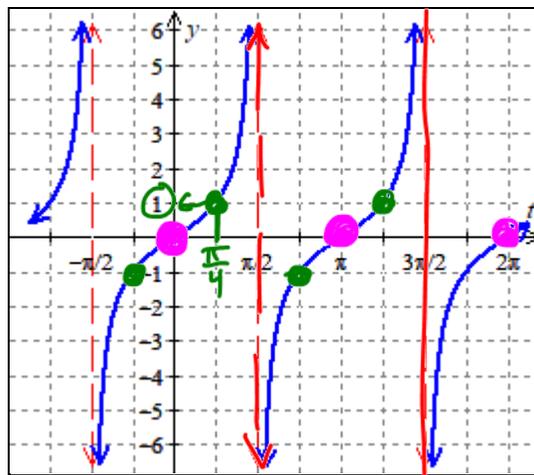
The **secant function** is defined by $\sec(t) = \frac{1}{\cos(t)}$.

The **cosecant function** is defined by $\csc(t) = \frac{1}{\sin(t)}$.

Below is the graph $y = \tan(t)$. Let's discuss why the graph looks like it does.

$y = \tan(t) = \frac{\sin(t)}{\cos(t)}$

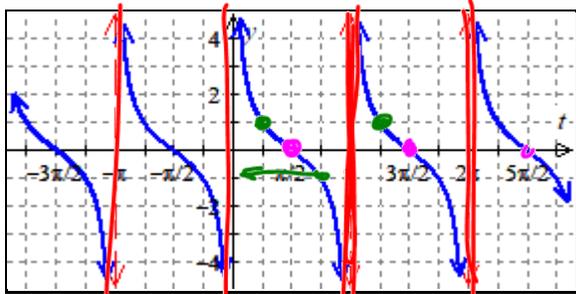
Since tangent involves division, tangent has "problems" where $\cos(t) = 0$, $\tan(t)$ is und.



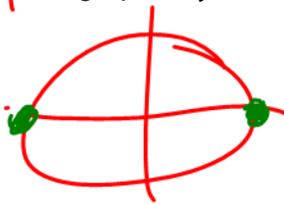
A graph $y = \tan(t)$.

$\tan(t) = 0 \implies \sin(t) = 0$

Below is the graph of $y = \cot(t)$. Let's discuss why it looks like it does.



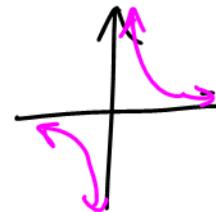
A graph of $y = \cot(t)$.



$$\cot(t) = \frac{\cos(t)}{\sin(t)}$$

$\sin(t) = 0 \Rightarrow \cot(t)$ is und

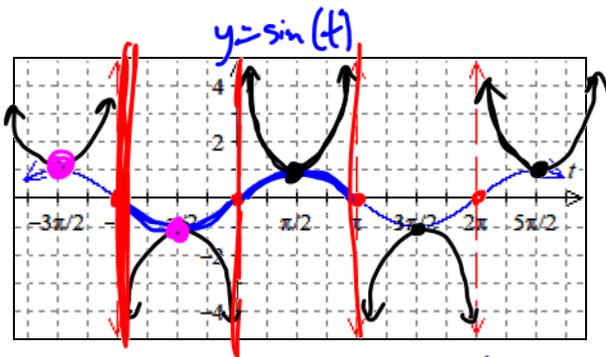
$$y = \frac{1}{x}$$



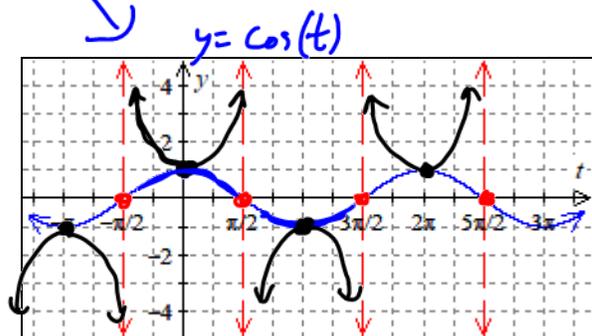
Let's sketch graphs of $y = \sec(t)$ and $y = \csc(t)$.

$$y = \sec(t) = \frac{1}{\cos(t)}$$

$$y = \csc(t) = \frac{1}{\sin(t)}$$



Draw a graph of $y = \csc(t)$



Draw graph of $y = \sec(t)$