

## Technical Definition of Functions

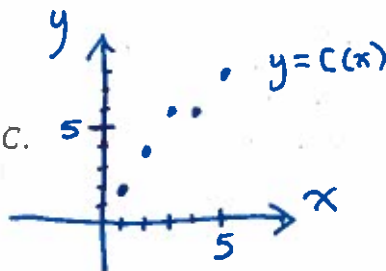
Work within a small group to answer these questions. Do not race through the exercises on your own. Always make sure that your entire group feels good about a question and answer before you move to the next exercise. Ask your group mates for explanations if you feel uncertain about something, and offer your explanations to others when you understand an exercise but someone else may not.

1. A function named  $C$  is given by  $\{(1, 2), (2, 4), (3, 6), (4, 6), (5, 8)\}$ .

- a) What are the domain and range of  $C$ ? Give your answers using set notation (with the curly braces).

domain of  $C$  is  $\{1, 2, 3, 4, 5\}$   
range of  $C$  is  $\{2, 4, 6, 8\}$

- b) Graph  $C$ .



- c) What is  $C(2)$ ? What is  $C(6)$ ?

undefined  
(6 is not in the domain of  $C$ )

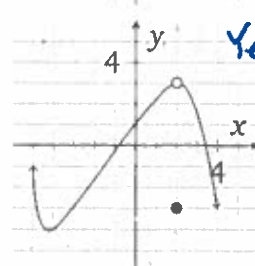
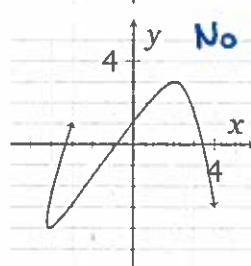
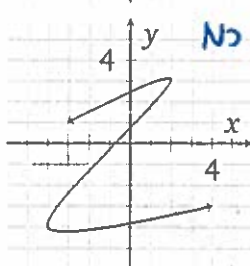
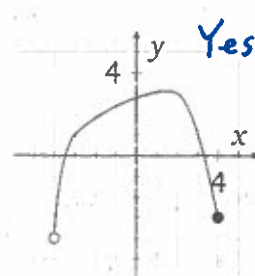
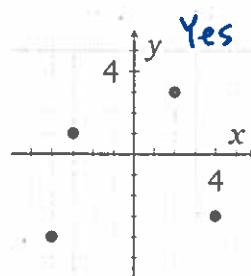
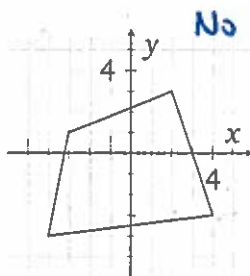
- d) Solve the equation  $C(x) = 8$ .

The only solution  
is  $x = 5$

- e) Solve the equation  $C(x) = 0$ .

there are no  
solutions.

2. Here are some graphs that give relations between  $x$  and  $y$ . Your job is to determine if the relation can be used to define  $y$  as a function of  $x$ . For each graph, after you make your decision, say a little bit about why. If you decide that the relation *can* be used to define a function, then you can just say that. But if it *cannot*, then give a reason why. For example, you might say something like "There is more than one possibility for what  $f(2)$  would be."



3. Which of these tables describe  $y$  as a function of  $x$ ? For each table, after you make your decision, say a little bit about why. If you decide that the relation *can* be used to define a function, then you can just say that. But if it *cannot*, then give a reason why. For example, you might say something like "There is more than one possibility for what  $f(2)$  would be."

| $x$ | $y$ | $x$ | $y$ | $x$ | $y$ | $x$ | $y$ | $x$ | $y$ | $x$    | $y$     |
|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|--------|---------|
| 1   | -12 | 10  | 3   | -12 | 9   | 2   | -2  | 3   | -1  | red    | Mercury |
| 2   | 10  | 15  | 4   | 10  | 8   | 4   | 17  | 8   | 10  | orange | Venus   |
| 3   | 8   | 20  | 3   | 8   | 3   | 5   | 1   | 7   | 14  | yellow | Earth   |
| 4   | 5   | 25  | 4   | 5   | -2  | 8   | 8   | 7   | 14  | green  | Mars    |
| 5   | 13  | 30  | 3   | 13  | 1   | 4   | 13  | 12  | 13  | blue   | Jupiter |
| 6   | 11  | 35  | 4   | 11  | 1   | 5   | 10  | 16  | -9  | purple | Saturn  |

Yes

Yes

Yes

No  
because  
what would  
 $f(5)$  be

Yes

Yes if you  
allow an abstract  
version of functions  
that don't use  
numbers as  
inputs &  
outputs.

4. For each of these relations between  $x$  and  $y$ , decide if  $y$  is a function of  $x$ .

a)  $y = 3x - 2$

Yes

b)  $2y = 3x - 2$

Yes

c)  $y^2 = 3x - 2$

No

d)  $x^2 + y^2 = 4$

No

e)  $|x| - y^2 = x^2$

No

f)  $y = \pm\sqrt{x}$

No

5. Let  $x$  represent the height of a person, and  $y$  represent their weight. Is  $y$  a function of  $x$ ? If not, explain why not.

No. You could have the same height ( $x$ ) twice, but  
they would be matched with two different weights ( $y$ ).

6. Let  $x$  represent the weight of a (1 foot)  $\times$  (1 foot)  $\times$  (1 foot) package you want to send through the postal service, and  $y$  represent the cost to ship it. Is  $y$  a function of  $x$ ? If not, explain why not.

Yes! For example  
a 10-lb. box won't  
cost two different amountscost  
as outputweight  
as input

7. In the same scenario as the previous question, is  $x$  a function of  $y$ ? If not, explain why not.

Suppose a package costs  
\$10 to ship, it's possible  
there is more than one weight  
associated  
with \$10.weight  
as outputcost  
as input

No!