

1.	$a$ and $b$	$x$ -coordinate	$y$ -coordinate	Vertex
a.	$a = 1$ $b = -7$	$x = -\frac{b}{2a}$ $= -\frac{-7}{2(1)}$ $= 3.5$	$y = 3.5^2 - 7(3.5) + 11$ $= -1.25$	$(3.5, -1.25)$
b.	$a = -2$ $b = -12$	$x = -\frac{b}{2a}$ $= -\frac{-12}{2(-2)}$ $= -3$	$y = -2(-3)^2 - 12(-3) - 50$ $= -32$	$(-3, -32)$
c.	$a = 1$ $b = -8$	$x = -\frac{b}{2a}$ $= -\frac{-8}{2(1)}$ $= 4$	$y = 4^2 - 8(4) - 9$ $= -25$	$(4, -25)$
d.	$y = (3x + 8)^2$ $= 9x^2 + 48x + 64$  $a = 9$ $b = 48$	$x = -\frac{b}{2a}$ $= -\frac{48}{2(9)}$ $= -\frac{8}{3}$	$y = \left(3\left(-\frac{8}{3}\right) + 8\right)^2$ $= 0$	$\left(-\frac{8}{3}, 0\right)$

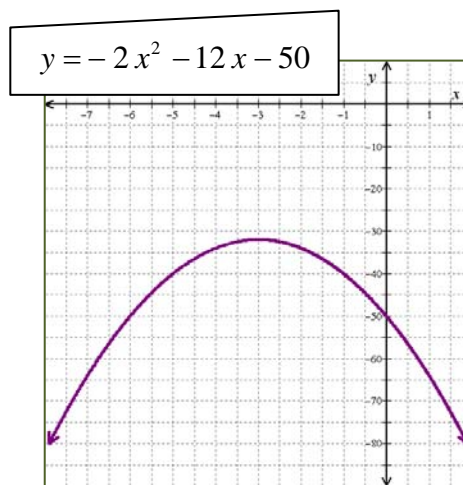
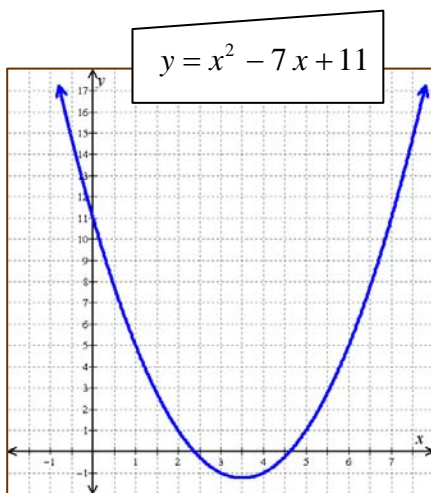
**Please note:** Fractional answers would be fine and dandy for question 1 (a). Decimal answers would not be acceptable for 1 (d) because the decimals would not be exact.

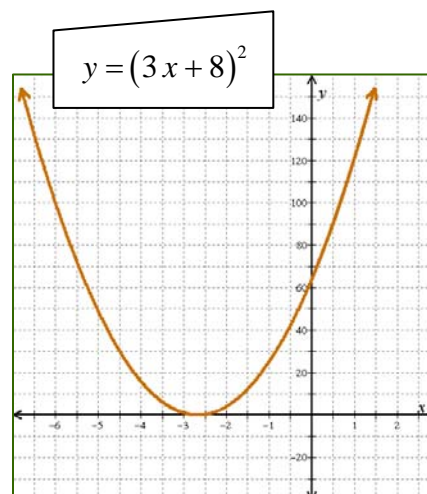
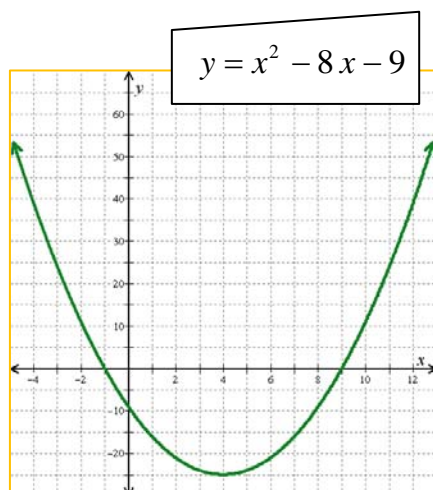
2. Find the intercepts of each parabola.

a.	$x^2 - 7x + 11 = 0$  $a = 1$ $b = -7$ $c = 11$	$x = \frac{-(-7) \pm \sqrt{(-7)^2 - 4(1)(11)}}{2(1)}$  $= \frac{7 \pm \sqrt{5}}{2}$	The $x$ -intercepts are:  $\left(\frac{7 + \sqrt{5}}{2}, 0\right)$ and $\left(\frac{7 - \sqrt{5}}{2}, 0\right)$ .  The $y$ -intercept is $(0, 11)$
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b.	$-2x^2 - 12x - 50 = 0$ $-\frac{1}{2}(-2x^2 - 12x - 50) = -\frac{1}{2}(0)$ $x^2 + 6x + 25 = 0$ $a = 1$ $b = 6$ $c = 25$	$x = \frac{-6 \pm \sqrt{6^2 - 4(1)(25)}}{2(1)}$ $= \frac{-6 \pm \sqrt{-64}}{2}$ <p>These are not real numbers!!</p>	<p>There are no <math>x</math>-intercepts!</p> <p>The <math>y</math>-intercept is <math>(0, -50)</math></p>
c.	$x^2 - 8x - 9 = 0$ $(x - 9)(x + 1) = 0$ $x - 9 = 0$ or $x + 1 = 0$ $x = 9$ or $x = -1$	<p>The <math>x</math>-intercepts are <math>(9, 0)</math> and <math>(-1, 0)</math>.</p> <p>The <math>y</math>-intercept is <math>(0, -9)</math></p>	
d.	$(3x + 8)^2 = 0$ $3x + 8 = 0$ $x = -\frac{8}{3}$	<p>The only <math>x</math>-intercept is <math>(-\frac{8}{3}, 0)</math>.</p> <p>When <math>x = 0</math>, <math>y = (0 + 8)^2 = 64</math>.</p> <p>The <math>y</math>-intercept is <math>(0, 64)</math>.</p>	

3.





4. The maximum height reached by the pits can be determined by finding the vertex of the parabola  $h(t) = -16t^2 + 32t + 48$ .

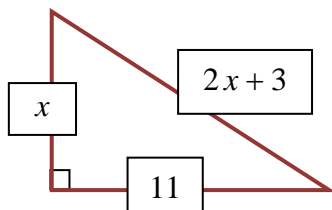
$a = -16$  and  $b = 32$  so the  $t$ -coordinate of the vertex is  $t = -\frac{32}{2(-16)} = 1$ . This tells us that it only took one second for the pita to reach its maximum height. The maximum height is determined by  $h(1) = 64$ . So the maximum height reached by the pita was 64 feet.

The pita hit the ground when  $h(t) = 0$ .

$$\begin{aligned} -16t^2 + 32t + 48 &= 0 \\ -\frac{1}{16}(-16t^2 + 32t + 48) &= -\frac{1}{16}(0) \\ t^2 - 2t - 3 &= 0 \\ (t - 3)(t + 1) &= 0 \\ t = 3 \text{ or } t = -1 \end{aligned}$$

Since the nasty pita didn't hit the ground before Abdou tossed it in the air, it must have take 3 seconds for the pita to reach the ground once it had been tossed by Abdou.

5. Let  $x$  represent the length of the unknown leg (measured in inches). Then the length of the hypotenuse is  $2x + 3$  and from the Pythagorean Theorem we get  $x^2 + 11^2 = (2x + 3)^2$ .



$$\begin{aligned}
 x^2 + 11^2 &= (2x + 3)^2 & a &= 3 & x &= \frac{-12 \pm \sqrt{12^2 - 4(3)(-112)}}{2(3)} \\
 x^2 + 121 &= 4x^2 + 12x + 9 & b &= 12 \\
 0 &= 3x^2 + 12x - 112 & c &= -112 & &= \frac{-12 \pm \sqrt{1488}}{6}
 \end{aligned}$$

$$\frac{-12 + \sqrt{1488}}{6} \approx 4.4 \text{ and } \frac{-12 - \sqrt{1488}}{6} \approx -8.4$$

Since the length of a right triangle leg surely can't be negative, the unknown leg length must be about 4.4 inches. This makes the hypotenuse length about 11.8 inches.

#### Check

$$4.4^2 + 11^2 = 140.36 \text{ and } 11.8^2 = 139.24$$

The answer checks ... the numbers are not exactly the same because of our rounding.